

Lesson 2-6: Systems of Inequalities I can solve a System of Linear Inequalities by Graphing.

I can Find the Minimum and Maximum of an Objective Function.

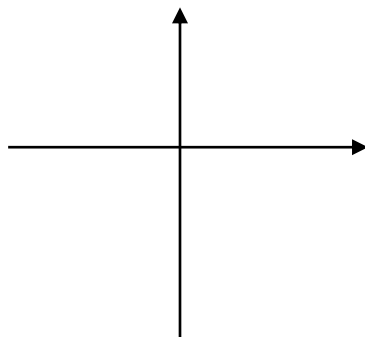
EQ: How do you solve a system of inequalities by graphing?

EX.1 - Solving a System by Graphing

Graph the system of Linear Inequalities.

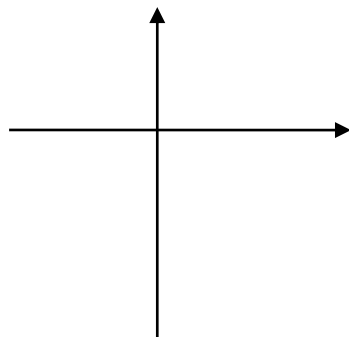
a.

$$\begin{cases} y > -2 \\ y \leq 1 \end{cases}$$



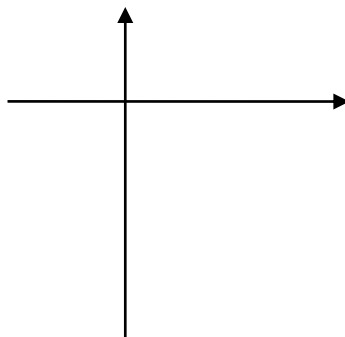
b.

$$\begin{cases} y > 2x - 7 \\ 4x + 4y < -12 \end{cases}$$



c.

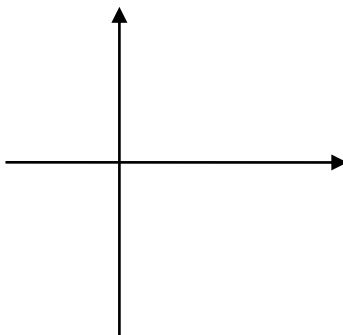
$$\begin{cases} y \geq -3x + 2 \\ 5x - 2y \leq -10 \end{cases}$$



Check (,)

d.

$$\begin{cases} y < 4 \\ y \geq |x - 3| \end{cases}$$



Steps for graphing a system of Linear Inequalities

1. Graph both corresponding lines. If the $<$ or $>$ use a dashed line; If the symbol is \leq or \geq use a solid line.
2. Determine which way to shade by checking a point away from each line. (plug it into the inequality)
 - If you get a yes, shade that direction
 - If you get a no, shade the other direction
2. Then shade (darken) the region that contains the common points
3. Check a point inside the shaded region to confirm your answer

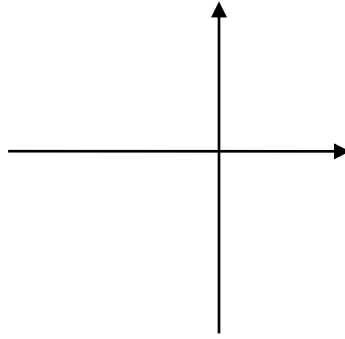
Lesson 2-6: Systems of Inequalities I can solve a System of Linear Inequalities by Graphing.

I can Find the Minimum and Maximum of an Objective Function.

EQ: How do you solve a system of inequalities by graphing?

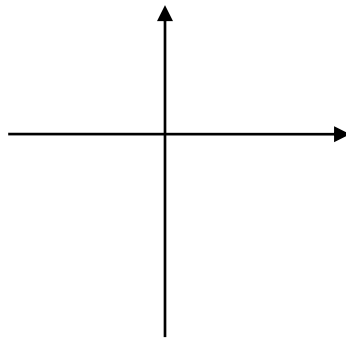
e.

$$\begin{aligned} y &\geq x \\ y &\leq |x + 5| - 2 \end{aligned}$$



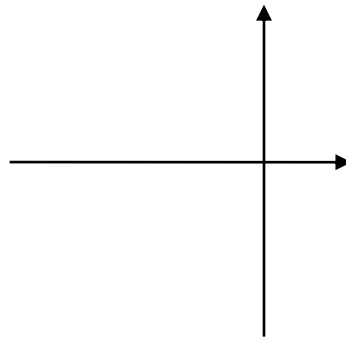
f.

$$\begin{aligned} y &\geq -2x + 4 \\ y &\leq |x - 4| \end{aligned}$$



g.

$$\begin{aligned} y &\geq 3 \\ y &> -|x + 2| + 5 \end{aligned}$$



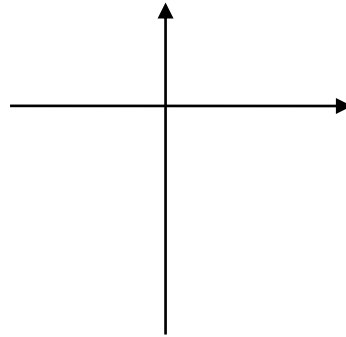
Lesson 2-6: Systems of Inequalities I can solve a System of Linear Inequalities by Graphing.

I can Find the Minimum and Maximum of an Objective Function.

EQ: How do you solve a system of inequalities by graphing?

h.

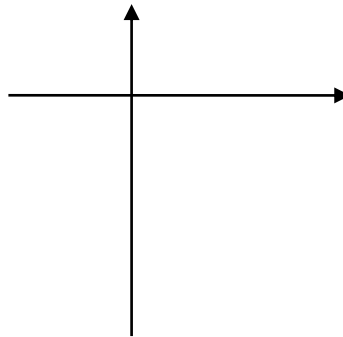
$$\begin{array}{l} -2 \leq x \leq 5 \\ y \geq 0 \\ y \leq 2x + 1 \end{array}$$



Check (,)

i.

$$\begin{array}{l} x \leq 0 \\ y + 3 \geq 0 \\ x \geq y \end{array}$$



Check (,)

Short Summary#1:

EX 2 – FINDING MAXIMUM AND MINIMUM

Vertex Theorem:

The **maximum** or **minimum** value of

$$f(x, y) = ax + by + c$$

on a polygonal convex set occurs at a vertex of the polygonal boundary.

Find the maximum and minimum value for each function with the given vertices.

a. $f(x, y) = 4x + 2y$

A(0, 0), B(0, -4), C(3, -5), & D(8, 0)

Lesson 2-6: Systems of Inequalities I can solve a System of Linear Inequalities by Graphing.

I can Find the Minimum and Maximum of an Objective Function.

EQ: How do you solve a system of inequalities by graphing?

b. $f(x, y) = x - 5y + 3$

J(1, 0), K(1, 9), L(6, -2), & M(8, 5)

c. $f(x, y) = 4y + 7x - 1$

R(-2, -1), S(-2, 0), T(-1, 10), U(3, 1) & V(7, 10)

EX.3 – Finding the Minimum and Maximum for a Polygonal Convex Set.

Find the maximum and minimum values for the polygonal convex set, defined by the system of inequalities.

a. $f(x, y) = 4x - 3y + 7$

$$x \geq 0$$

$$y \geq 1$$

$$x + y \leq 4$$

b. $f(x, y) = -2x + y + 5$

$$2 \leq y \leq 8$$

$$x \geq 1$$

$$2x + y \leq 14$$

$$y \geq 5 - x$$

Lesson 2-6: Systems of Inequalities I can solve a System of Linear Inequalities by Graphing.

I can Find the Minimum and Maximum of an Objective Function.

EQ: How do you solve a system of inequalities by graphing?

c. $f(x,y) = -2x + y + 5$

$$0 \leq x \leq 8$$

$$y \geq -1$$

$$y \leq 0.5x + 1$$

EX.4 - APPLICATION

1. An entrance exam has two parts, a verbal part and a mathematics part. You can score a maximum total of 1600 points. For admission, the school of your choice requires a math score of at least 600. Write a system of inequalities to model scores that meet the school's requirements. Then solve the system.

2. Another school requires a math score of at least 550 points and a total score of at least 1100 points. You can score up to 800 points on each part. Write and solve a system of inequalities to model scores that meet the school's requirements.

Lesson 2-6: Systems of Inequalities I can solve a System of Linear Inequalities by Graphing.

I can Find the Minimum and Maximum of an Objective Function.

EQ: How do you solve a system of inequalities by graphing?

3. Jenna spends at most 150 minutes a night on math and science homework. She spends at least 60 minutes on math. Write and solve a system of inequalities to model how she allots her time for these two subjects.

Short Summary #2:

Lesson 2-6: Systems of Inequalities I can solve a System of Linear Inequalities by Graphing.

I can Find the Minimum and Maximum of an Objective Function.

EQ: How do you solve a system of inequalities by graphing?